

CPSC 326 Problem Set 2

Due March 19

1. Given the following grammar G_1 :

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T \times F \mid F$$

$$F \rightarrow (E) \mid a \mid b \mid c$$

- What are the variables?
 - Which is the start variable?
 - What are the terminals?
 - How many productions does the grammar have?
2. Give parse trees for the following strings using grammar G_1 above:
- | | |
|---------------------|-----------------------|
| a. a | d. $(a + b) \times c$ |
| b. $a + b \times c$ | e. $((a))$ |
| c. $a \times b + c$ | f. $a + b + c$ |
3. Design a PDA which recognizes the same language as the grammar G_1 generates.

4. Create a context-free grammar which recognizes all strings of “properly-matched” parenthesis. The strings on the left are examples of properly-matched parenthesis, and should be produced from your grammar. The strings on the right are not properly matched and should not be produced:

Proper:

$()$

$()()$

$(())$

Improper:

$()$

$()()$

$()$

5. Create a push-down automaton which recognizes the language of properly-matched parenthesis.
6. Is the language of properly-matched parenthesis a regular language? Justify your answer.

7. Give context-free grammars for the following two languages:

a. $\{a^m b^n c^n \mid m, n \geq 0\}$

b. $\{a^n b^n c^m \mid m, n \geq 0\}$

8. Given your answers to the previous problem, and the fact that the language $\{a^n b^n c^n \mid n \geq 0\}$ is *not* context-free, are context-free languages closed under intersection? Explain your reasoning.

9. Show that context-free languages are closed under the regular operations of union, concatenation, and star.